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# **The Role of the Hospital Characteristics in Setting Appropriate Yardsticks for Hospital Profiling**

**November 5, 2013**

**Presentation to the Federal Committee on Statistical Methodology  
Research Conference  
Washington, DC  
Frank Yoon**

**MATHEMATICA  
Policy Research**

# Overview

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- **Recap: statistical model**
- **Illustration: Pneumonia mortality rate  
Inpatient Quality Indicator #20**
- **Look ahead: the role of hospital characteristics**
  - Risk adjustment
  - Stabilization

# Risk Adjustment

## Patient-level model

Patient  $i$ , event  $Y_i$ , attributes  $X_i$

$$Y_i | p_i \sim \text{Bernoulli}(p_i), \text{logit}(p_i) = X_i' \beta$$

## Hospital-level rates

Hospital  $h$ , patients  $A_h$ , volume  $n_h$

$$\text{Observed rate, } O_h = \frac{1}{n_h} \sum_{i \in A_h} Y_i$$

$$\text{Expected rate, } E_h = \frac{1}{n_h} \sum_{i \in A_h} \hat{Y}_i$$

## Risk-adjusted rate

$$RAR_h = \frac{O_h}{E_h} \cdot \bar{Y}, \text{ where } \bar{Y} = \frac{\sum_i Y_i}{N}$$

# Smoothing

## Signal extraction framework

$$\begin{aligned} RAR_h &= \theta_h + \epsilon_h \\ &= \text{signal} + \text{noise} \end{aligned}$$

where  $E(\theta_h) = \mu$ ,  $Var(\theta_h) = \tau^2$   
 $E(\epsilon_h) = 0$ ,  $Var(\epsilon_h) = \sigma_h^2$

# Smoothing

## Reliability weighting

$$\theta_h = \underbrace{\mu + \lambda_h \cdot (RAR_h - \mu)}_{\text{Smoothed rate}} + \omega_h$$

where  $E(\omega_h) = 0$ ,  $Var(\omega_h) < \infty$

## OLS

$$\lambda_h = \frac{Cov(\theta_h, RAR_h)}{Var(RAR_h)} = \frac{Var(\theta_h)}{Var(\theta_h) + Var(\epsilon_h)} = \frac{\tau^2}{\tau^2 + \sigma_h^2}$$

# Smoothing

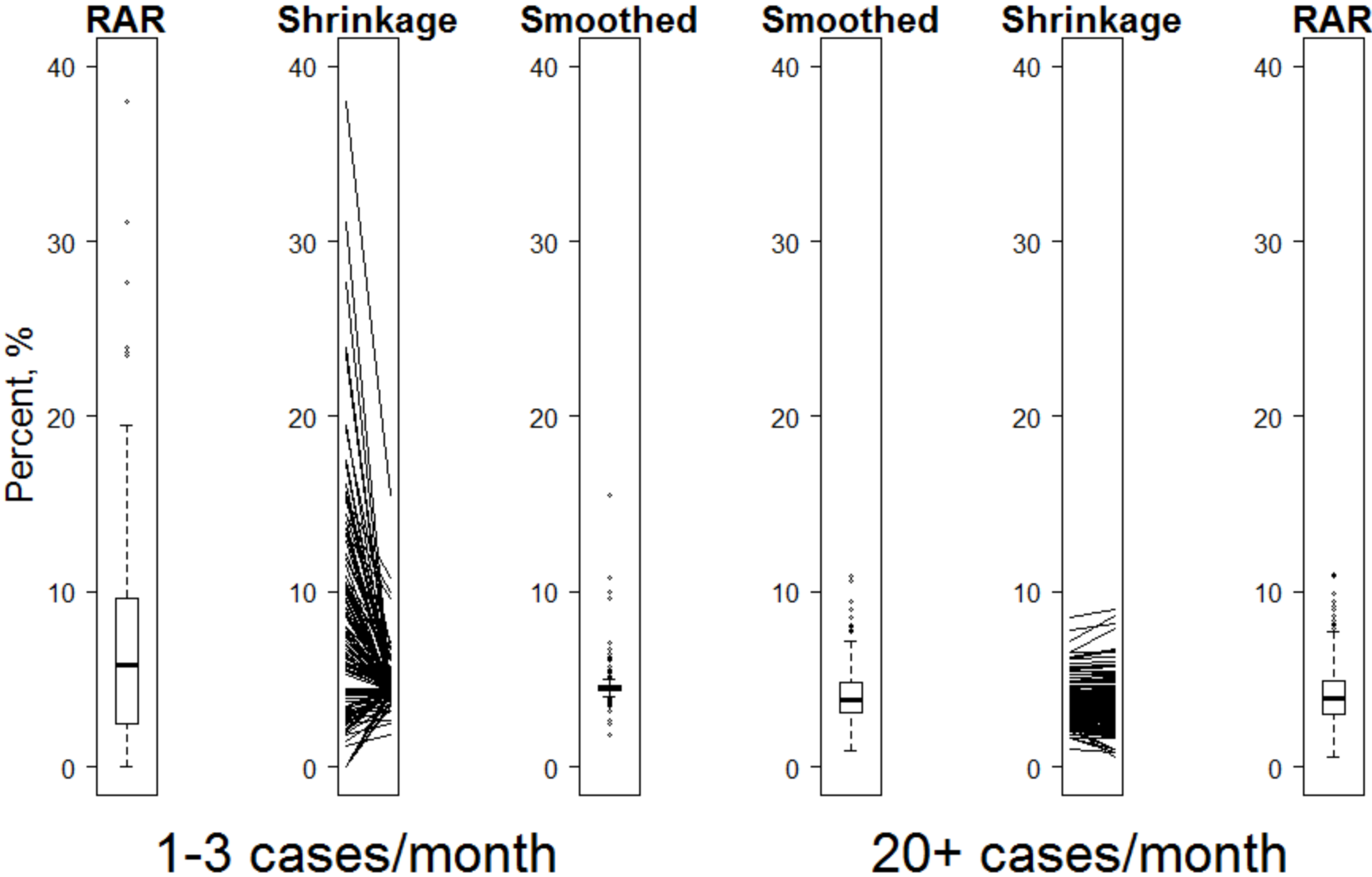
## Noise variance

$$\begin{aligned} \text{Var}(\epsilon_h) &\approx \text{Var}(RAR_h | \theta_h) \\ &= \text{Var}\left(\bar{Y} \cdot \frac{O_h}{E_h}\right) \\ \Rightarrow \hat{\sigma}_h^2 &= \left(\frac{\bar{Y}}{n_h \cdot E_h}\right)^2 \sum_{i \in A_h} \hat{Y}_i (1 - \hat{Y}_i) \end{aligned}$$

## Signal variance

$$\begin{aligned} \text{Var}(\theta_h) &= \text{Var}(RAR_h) - \text{Var}(\epsilon_h) \\ \Rightarrow \hat{\tau}^2 &= \frac{1}{H-1} \sum_h \left\{ (RAR_h - \overline{RAR})^2 - \hat{\sigma}_h^2 \right\} \end{aligned}$$

# Pneumonia Mortality Rate



# Statistical Context

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- **Risk adjustment**
  - Remove variation due to patient case mix
  - Recalibrate expectation of quality
  
- **Stabilization**
  - Smoothing unstable estimates might mask true variation
  - Prior assumptions play a big role
    - Bigger in low-information settings
    - Statistical challenge: what is the prior?



# Policy Context

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- **Risk adjustment**
  - Level the playing field
  - Certain hospital types may take on unobserved risk
- **Stabilization**
  - Small hospitals present unstable estimates
  - Variation in quality may depend on hospital type
  - Prior assumptions set different expectations
    - Empirically testable
    - Policy challenge: what is the message?

# Hospital Characteristics in Risk Adjustment

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## Patient-level model

Patient  $i$ , event  $Y_i$ , attributes  $X_i$ , hospital characteristics  $Z_h$

$$Y_i | p_i \sim \text{Bernoulli}(p_i)$$

$$\text{logit}(p_i) = X_i' \beta + Z_{h[i]}' \gamma$$

# Hospital Characteristics in Stabilization

## Signal extraction framework

$$RAR_h = \theta_h^* + \epsilon_h$$

where  $\theta_h^* = \theta_h + Z_h' \gamma$

$$E(\theta_h^*) = \mu + Z_h' \gamma, \quad \text{Var}(\theta_h) = \tau^2$$

$$E(\epsilon_h) = 0, \quad \text{Var}(\epsilon_h) = \sigma_h^2$$

# Potential Enhancements

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- **Empirical Bayes framework**
  - Elucidate assumptions about prior distribution
  - Achieve credible posterior inferences
- **Unified modeling**
  - Perform risk adjustment and stabilization in one fell swoop
  - Computationally feasible

# Empirical Bayes in Hospital Profiling

- **Decomposition of signal and noise**

$$RAR_h = \theta_h + \varepsilon_h$$

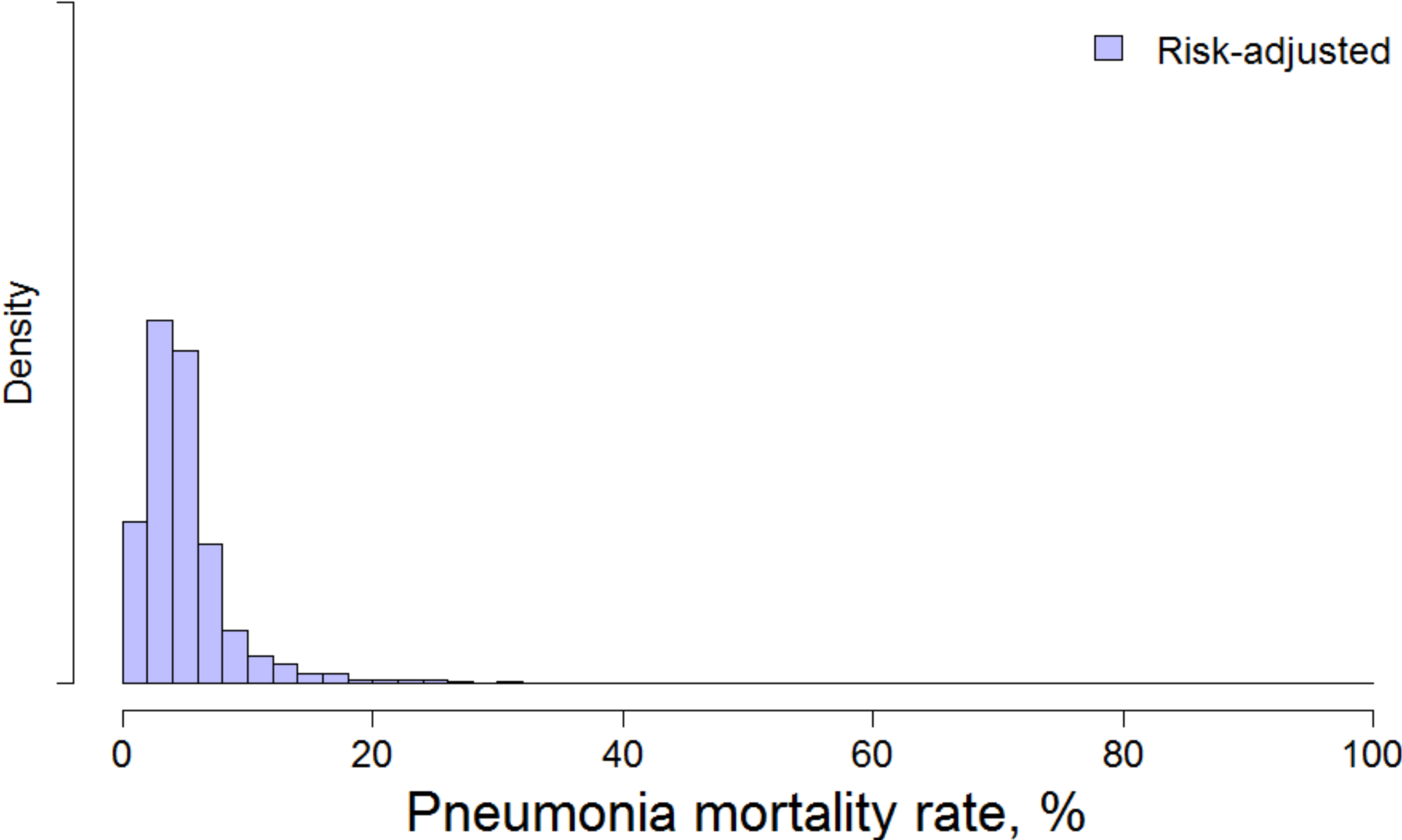
True rate  $\theta_h \sim \text{Prior}$

Error  $\varepsilon_h \sim N(0, \sigma_h^2)$

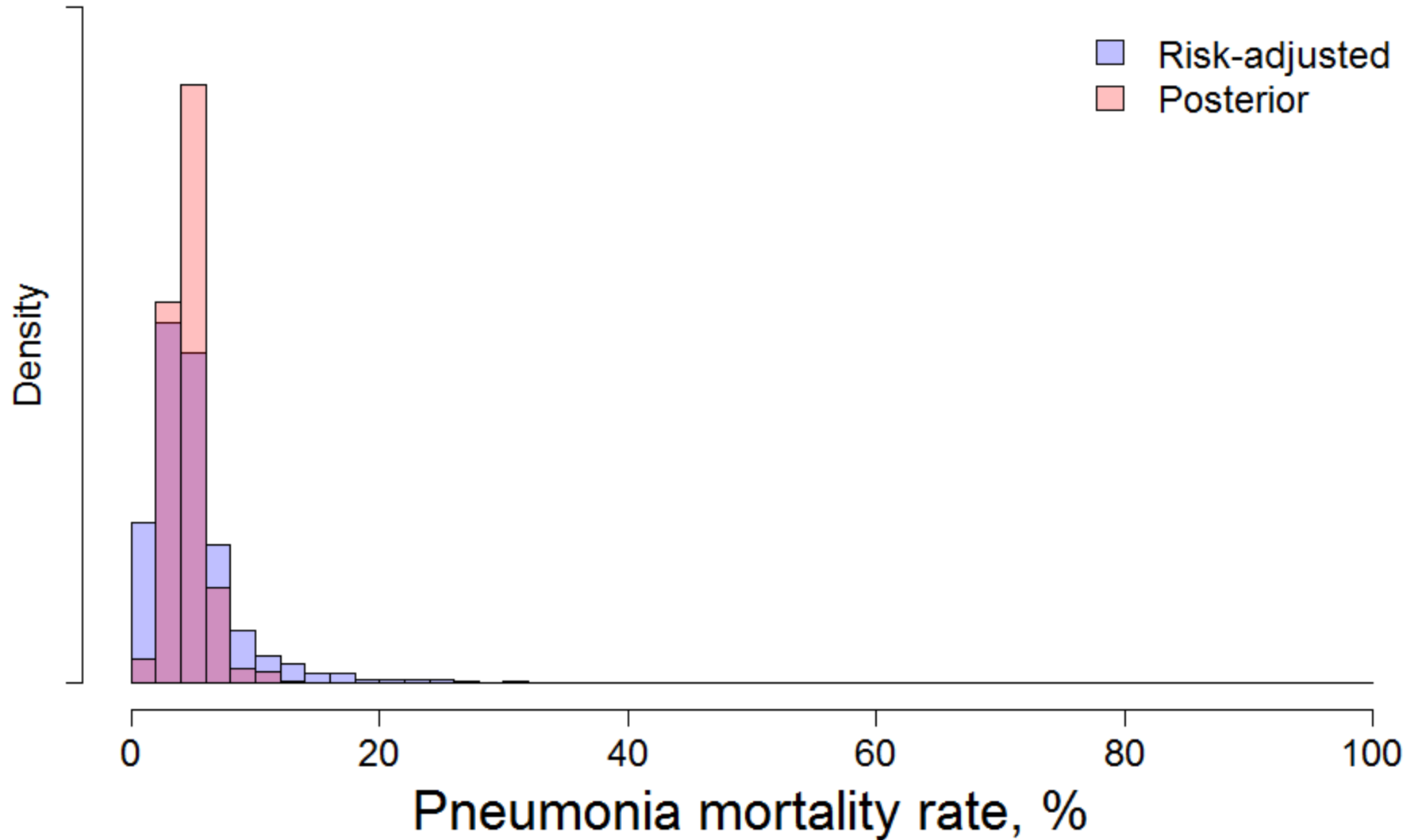
Data  $RAR_h | \theta_h$

Posterior  $\theta_h | RAR_h$

# Setting the Yardstick



# Yardstick from a Gamma Prior



# Addressing Overshrinkage

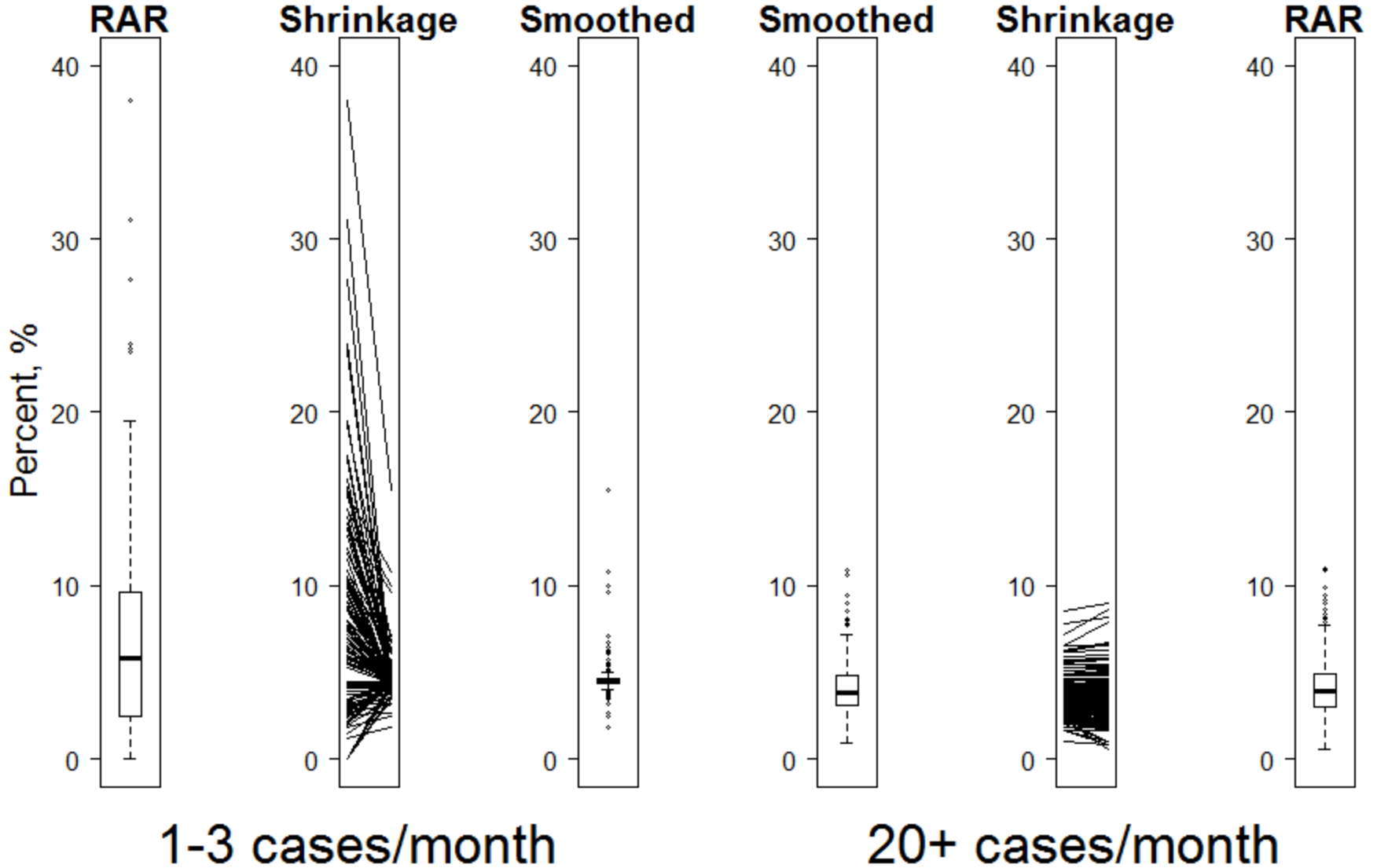
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**Does smoothing mask variation in true rate?**

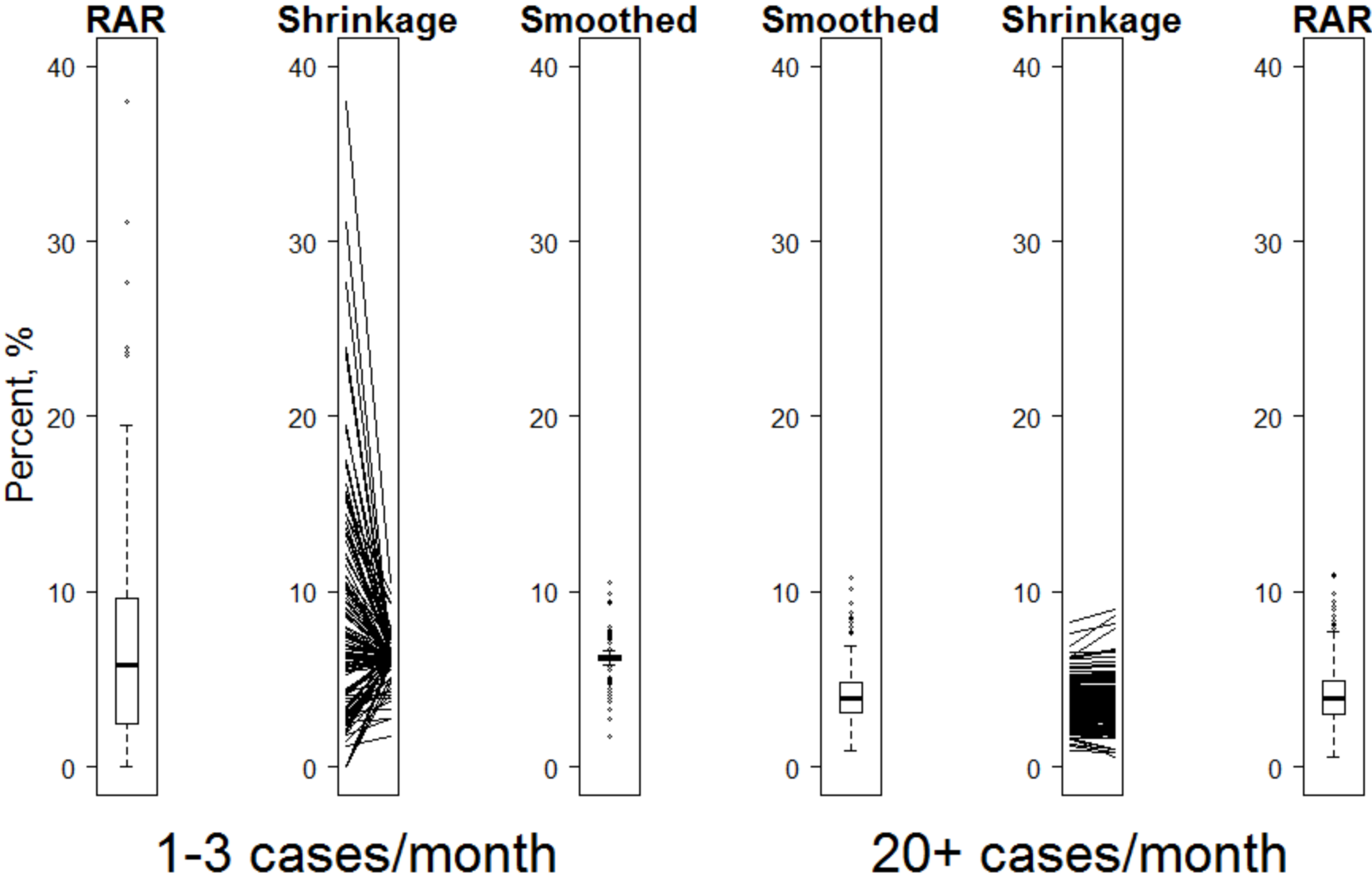
- **Restrictive prior distributions can hide possible outliers**
- **Prior means of true rate may or may not depend on peer grouping**
- **In the policy context expectations matter**



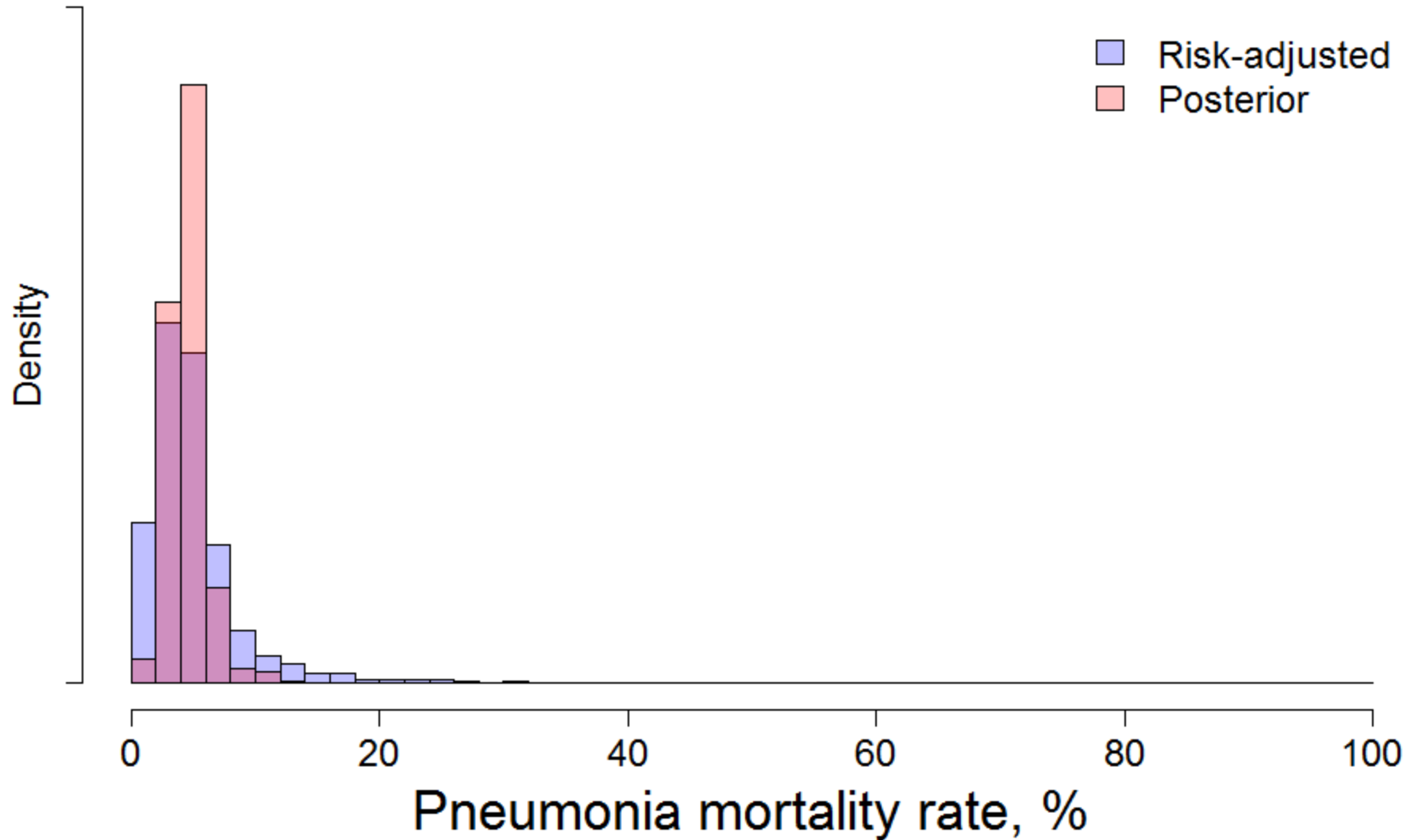
# The Effect of Stabilization



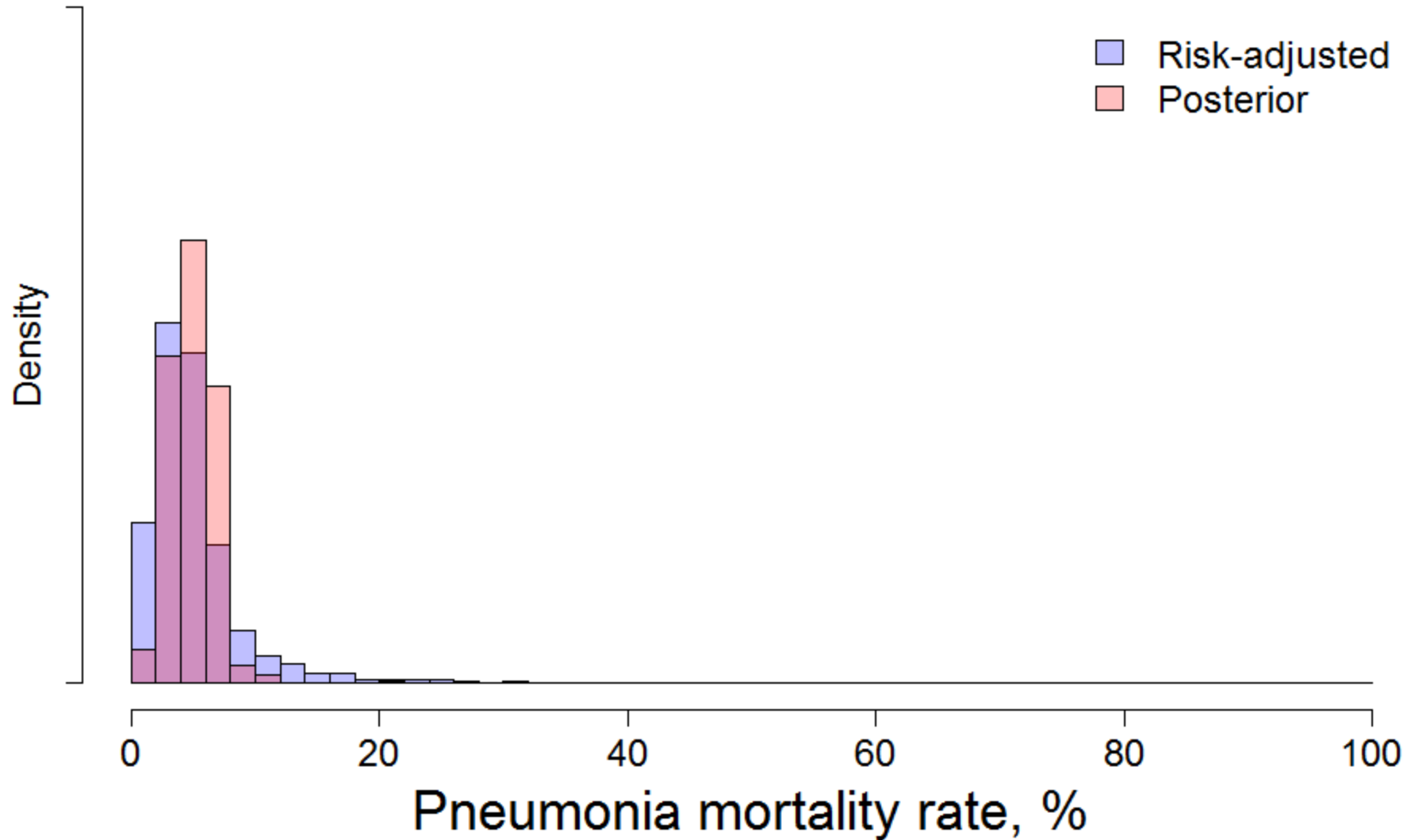
# Mixture of Normals by Volume Quintile



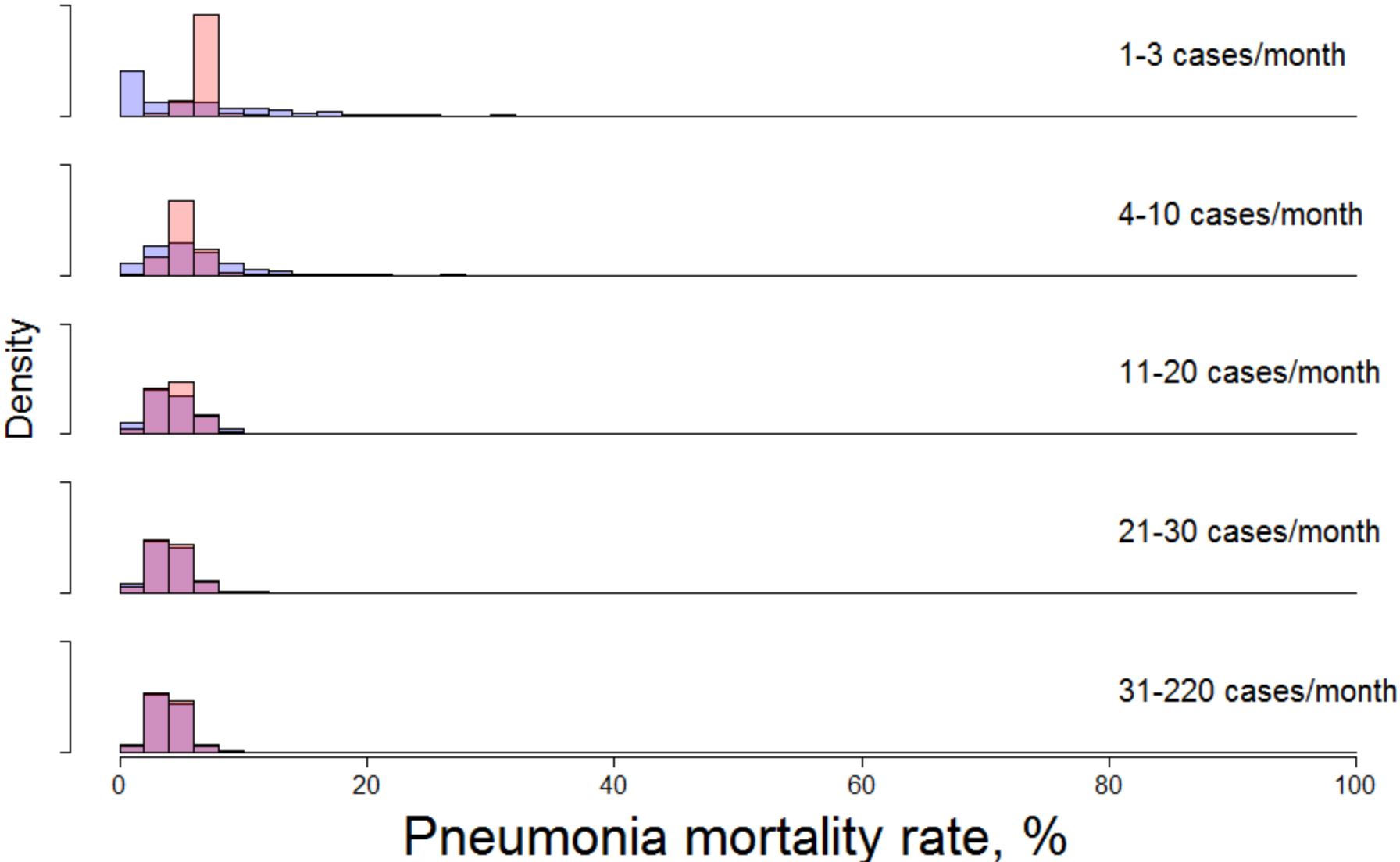
# Yardstick from a Gamma Prior



# Yardstick from Volume Peer Groups



# Peer Groups by Volume Quintiles



# Policy Implication

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- **It depends on the application**
  - Self-monitoring
  - Public reporting
  - Pay for performance
- **What is the message?**
  - Leveling the playing field in risk adjustment is not a testable exercise
  - Setting expectations via the prior is empirically justifiable, “potentially resolvable”

# Research Implications

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- **Standing by our prior, with or without peer grouping**
- **Empirical justification**
  - Literature review
  - Exploratory data analysis
  - Hypothesis driven
  - Simulation based

# For More Information

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