

# Evaluating Hot Deck with Propensity Score Matching For the Advance Monthly Retail Trade Survey (MARTS)

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# Outline

- Hot Deck
- Propensity Matching
- Relationship between Hot Deck Imputation and Propensity Matching
- Our Application
- Evaluation
- Concluding Remarks
- Related Research

# Hot Deck Imputation

- Often described as “model free”
- Donors – reported values
- Recipients – missing values
- Recipient and donor are matched
  - Direct substitution from donor

$$\text{Current Month Sales}_{\text{Recipient}} = \text{Current Month Sales}_{\text{Donor}}$$

- Derived from donor

$$\text{Current Month Sales}_{\text{Recipient}} =$$

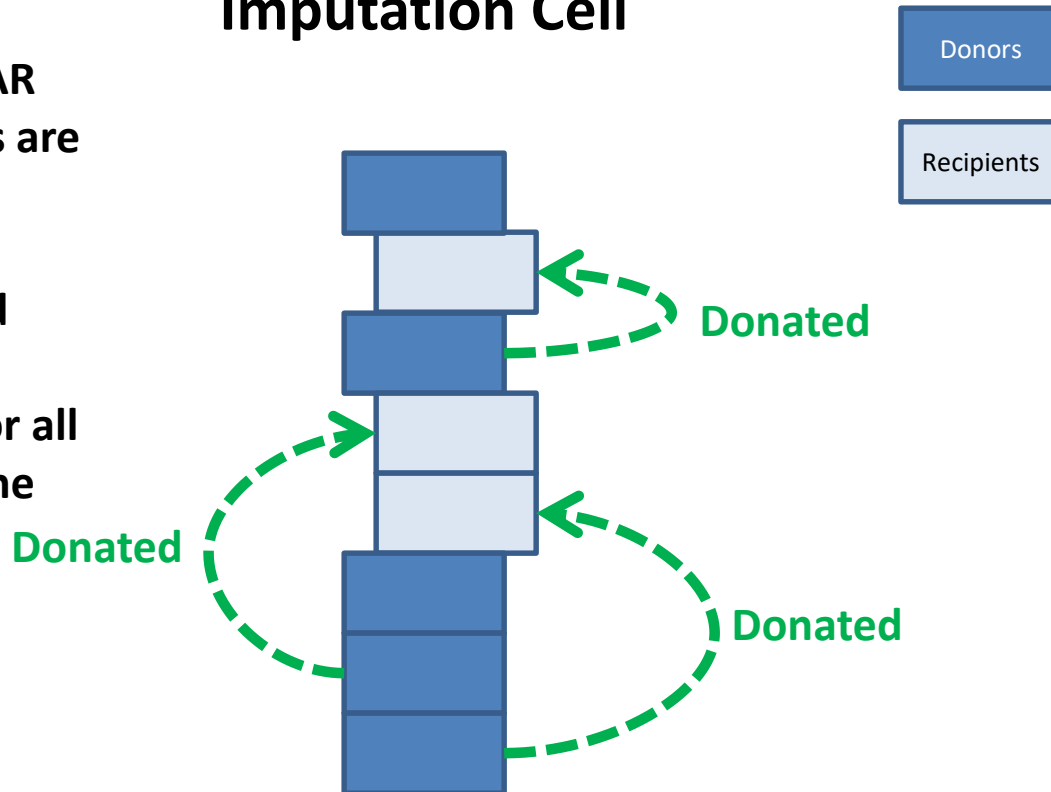
$$\frac{\text{Current Month Sales}_{\text{Donor}}}{\text{Previous Month Sales}_{\text{Donor}}} \text{Previous Month Sales}_{\text{Recipient}}$$

# Random Hot Deck

## Imputation Cell

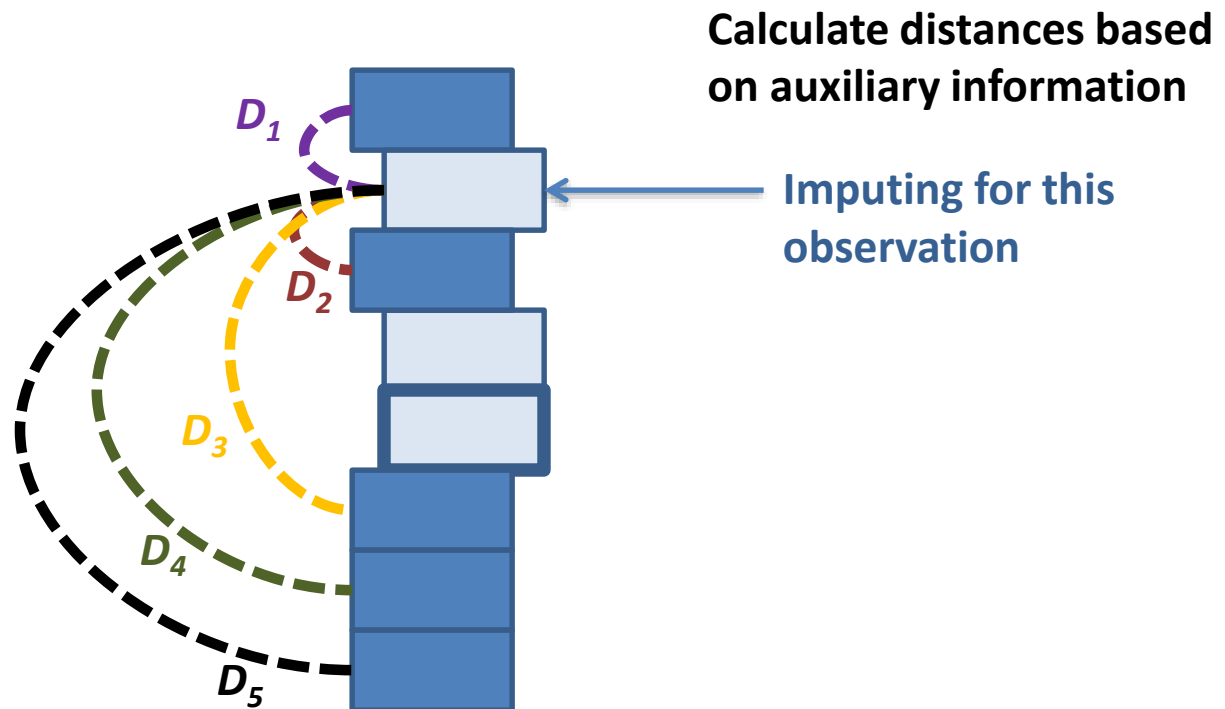
Assumes MCAR or MAR when imputation cells are used.

Assumes the expected value of outcome of interest is the same for all observations within the imputation cell.



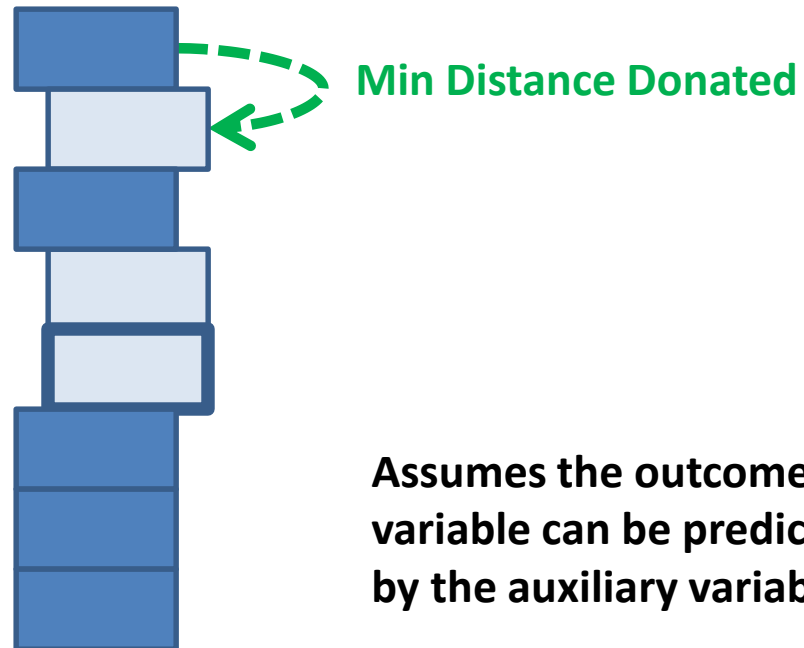
# Nearest Neighbor Hot Deck

## Imputation Cell



# Nearest Neighbor Hot Deck

## Imputation Cell



**Assumes the outcome variable can be predicted by the auxiliary variables**

# Hot Deck With Business Surveys

- Skewed population
  - Direct donation not a good idea for quantitative variables
  - Nearest Neighbor often used (size predictive of response/outcome)
- Derived value – donor ratio
- More recipients than donors
- Seasonal effects/trading day effects

# Propensity Score Matching

- Background
  - Causal inference/causal assumptions
  - Predicting outcome variable (response to treatment due to factors that are common to both treatment and control)
- Propensity Score
  - One single score or combinations of variables



# What About Propensity Scoring?

How do you develop one appropriate score function?

Everything into the score (all variables)

Compromise between the two methods

Develop a score within a block

What about important continuous variables?

No score (block)

# How propensity scoring works

- Matching
  - Need to specify a distance function.
  - Cannot re-use donors (one to one or many to one).
- Greedy matching<sup>1</sup>
  - Pairs donors to recipients sequentially.
  - Sort matters (confounding with distance).
  - Need to have more donors than recipients to use.
- Optimal matching<sup>1</sup>
  - Pairs donors to recipients based on closest distance subject to minimizing total aggregated distance over all recipients.
  - Distance function matters.

<sup>1</sup>Used publicly available SAS code developed by Bergstralh and Kosanke at the Mayo Clinic (<http://www.mayo.edu/research/departments-divisions/departments-health-sciences-research/division-biomedical-statistics-informatics/software/locally-written-sas-macros>)

# Greedy matching

Recipients sorted in ascending sequence

Distance between donor W and Recipient A is 7


Donor Y is matched with Recipient A

	Donors			
Recipients	W	X	Y	Z
A	7	8	<b>5</b>	13
B	10	9	4	<b>6</b>
C	<b>11</b>	17	8	10
D	25	<b>14</b>	7	8


# Greedy matching

	Donors			
Recipients	W	X	Y	Z
A	7	8	5	13
→ B	10	9	4	6
C	11	17	8	10
D	25	14	7	8

# Greedy matching

	Donors			
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# Greedy matching

	Donors			
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C	<b>11</b>	17	8	10
 D	25	<b>14</b>	7	8

# Greedy matching – sort matters

Recipients sorted in descending sequence

Donor W is matched with Recipient A

	Donors			
Recipients	W	X	Y	Z
D	25	14	<b>7</b>	8
C	11	17	8	<b>10</b>
B	10	<b>9</b>	4	6
A	<b>7</b>	8	5	13

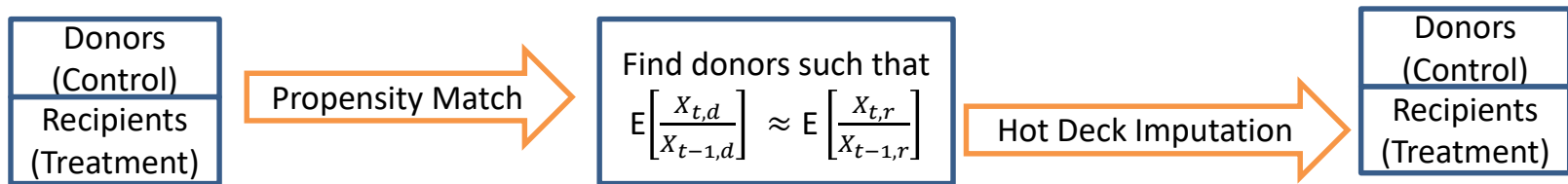
# Optimal matching

Donor X is matched with Recipient A

	Donors			
Recipients	W	X	Y	Z
A	7	<b>8</b>	5	13
B	10	9	<b>4</b>	6
C	<b>11</b>	17	8	10
D	25	14	7	<b>8</b>



# Relationship between hot deck and propensity matching



Causal inference framework:

- Treatment = donor selection procedure
- Block = imputation cell
- Outcome = M-T-M change

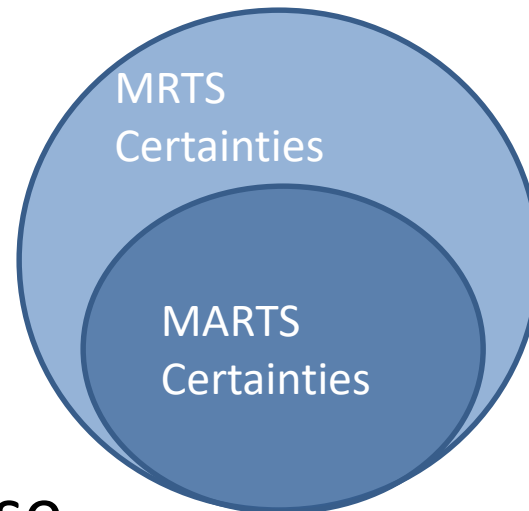
# Our application - Advance Monthly Retail Trade Survey (MARTS)

- Monthly Economic Indicator
  - Sales and month-to-month percent change
  - Inputs into the quarterly Gross Domestic Product (GDP) produced by the Bureau of Economic Analysis
- MARTS is a subsample of Monthly Retail Trade Survey (MRTS)
  - Certainties – selected with probability = 1

	MARTS	MRTS
Sample size	5,000 companies	12,000 companies
Sample frame	MRTS sample	Annual Retail Trade Survey sample
Sample design	Stratified PPS -WOR (subsample of MRTS)	Stratified SRS-WOR
Sample redesign cycle	Approximately every 2.5 years	Approximately every 5 years
Time to respond	Approximately 7 business days	Approximately 5 weeks
Imputation	Analyst impute for selected companies	Analyst imputes retained, ratio impute for remaining nonrespondents and edit-failing items
Estimation	Link relative estimator	Horvitz-Thompson estimator
Tabulation industries	30	83

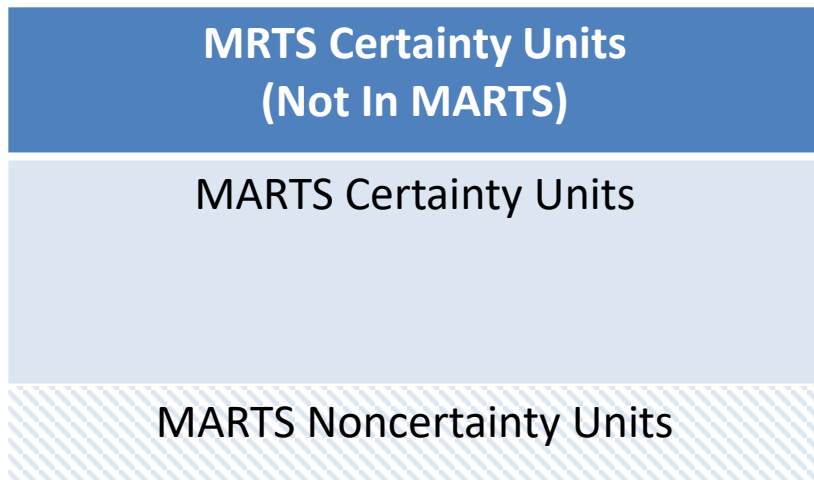
# Our application - Advance Monthly Retail Trade Survey (MARTS)

- The largest MRTS Certainties are selected with certainty for MARTS



- Low Response Rates & Size is Predictive of Response
- Data are seasonally adjusted
  - Seasonal effects
  - Trading day effects – many series

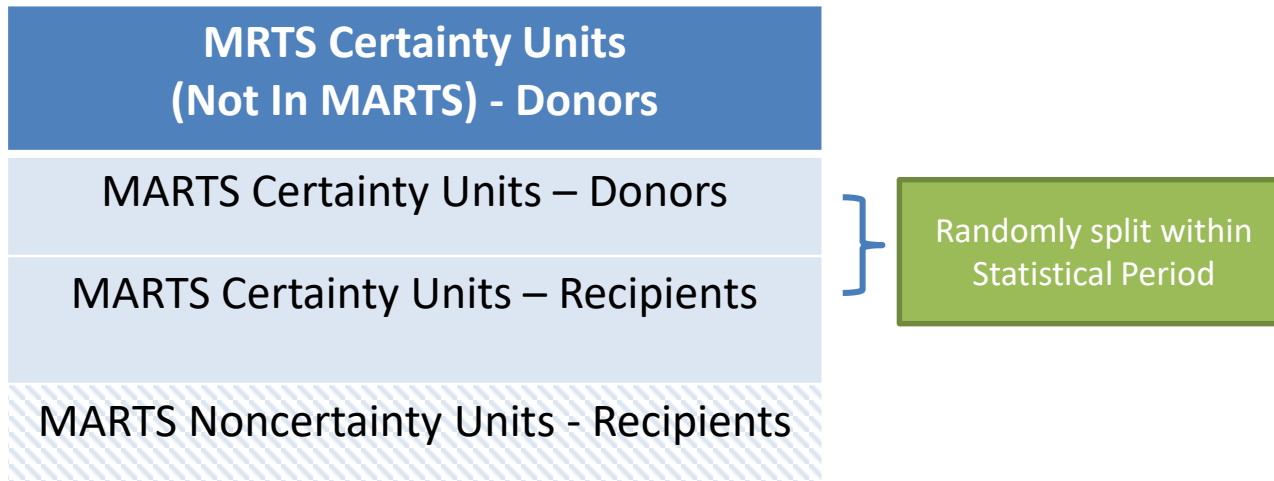
# Simulation Study Design



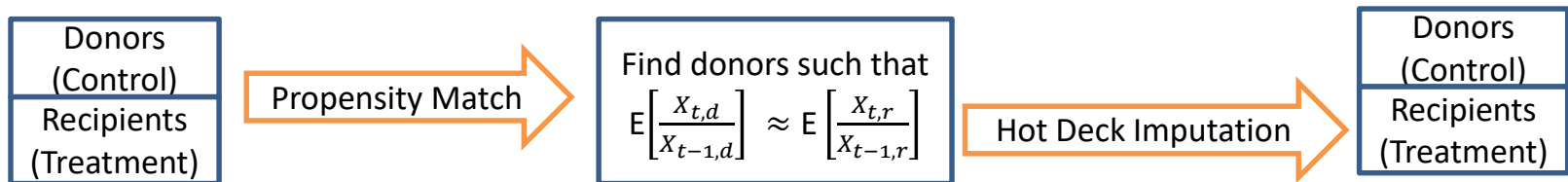
## Source Data:

- In Statistical Period
  - March 2016 – Feb. 2017
- MRTS Certainty Units ONLY
- Responded to MRTS
  - Current Period and Prior Period
  - Both values of sales  $> 0$

# Simulation Study Design



# Relationship between hot deck and propensity matching



Causal inference framework:

- Treatment = donor selection procedure
- Block = imputation cell
- Outcome = M-T-M change

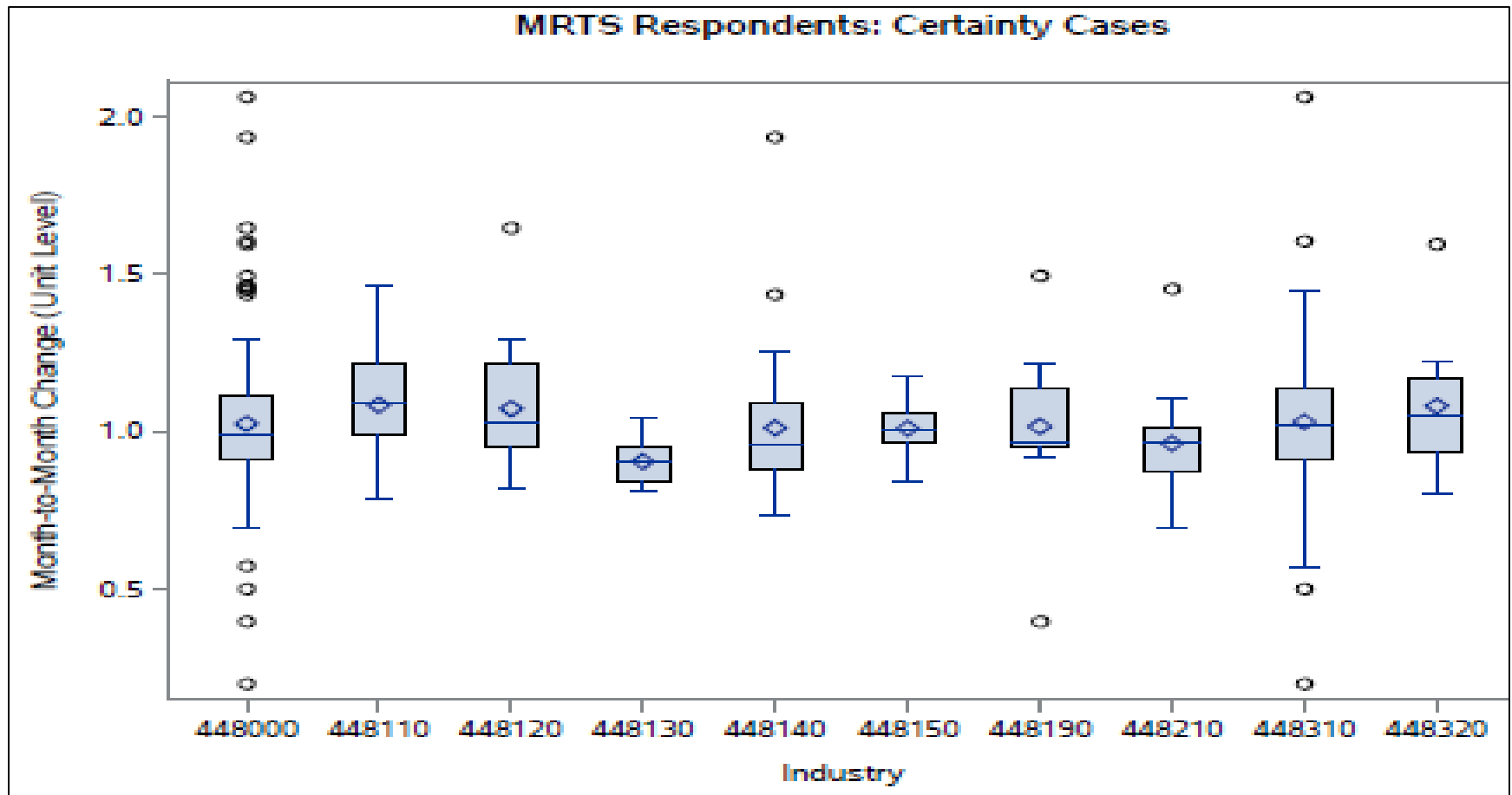
What should our match variables be?

# Finding Matching Variables

- What variables are predictive of month-to-month change?
  - Industry – 6-digit NAICS (North American Industry Classification System) vs 3-digit NAICS



# Distributions of Month-to-Month Change in NAICS 448

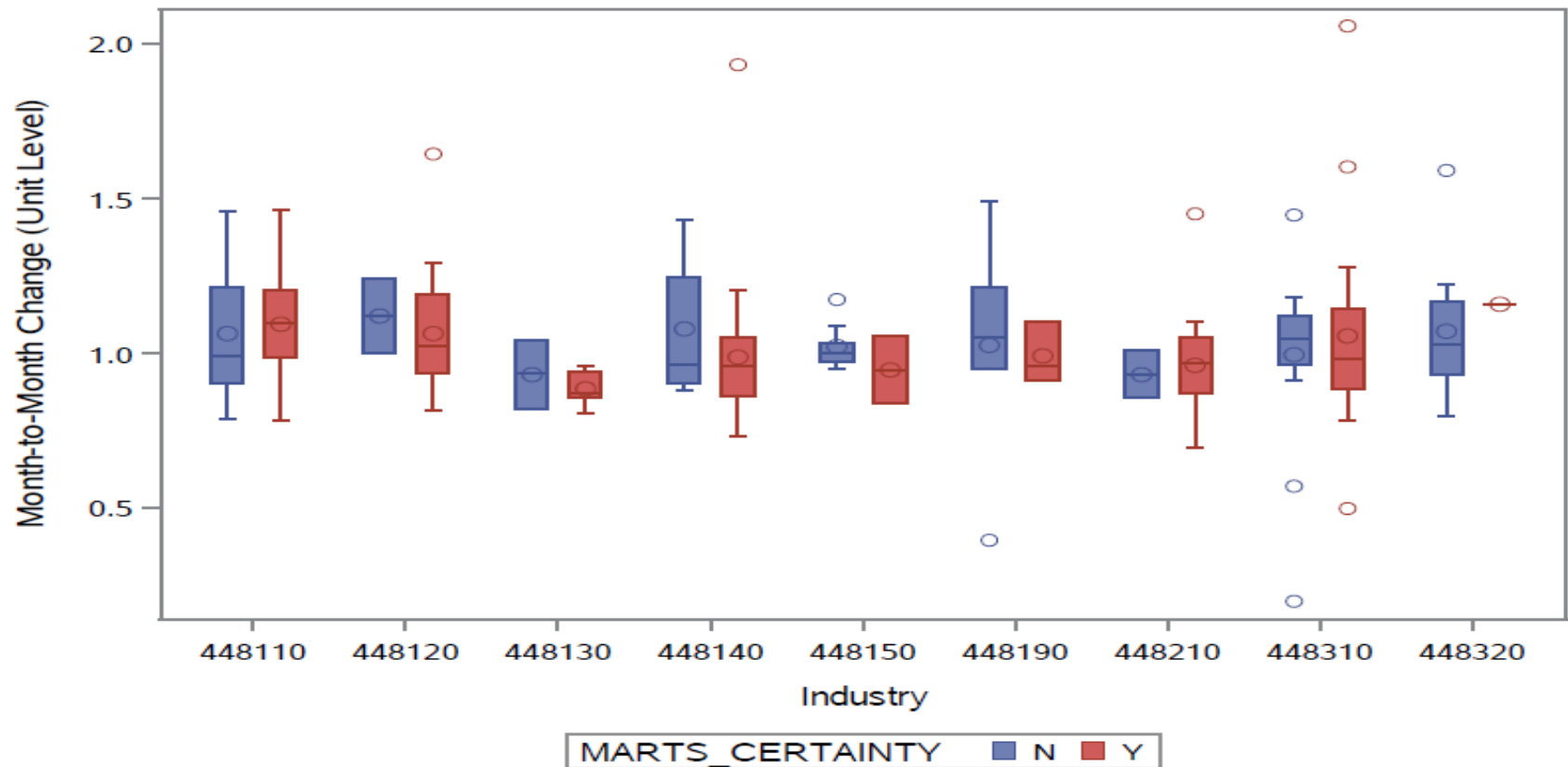


# Finding Matching Variables

- What variables are predictive of month-to-month change?
  - A lot is built into the imputation cells
    - Industry – 6-digit NAICS (North American Industry Classification System) vs 3-digit NAICS
  - Unit size

# Distributions of Month-to-Month Change in NAICS 448

MRTS Respondents: Certainty Cases in NAICS 448  
By MARTS Certainty and Noncertainty Status



# Finding Matching Variables

- Predictive of m-t-m change
  - A lot is built into the imputation cells
    - Industry – 6-digit NAICS (North American Industry Classification System) vs 3-digit NAICS
  - Unit size is important – but we are restricted to MRTS certainty only (historic data limitations)
- Other factors investigated
  - Prior month sales (size)
  - Sampling weight (size)
  - Variables predictive of response

# Actual Matches

- Blocks/Imputation Cells – 6-digit industry
- Matching variables
  - Prior month sales
  - Number of industries that the company operates in (proxy for complexity of the company)

# Evaluation

		Hot deck method	Match Variables	Sort Variables
<b>Greedy</b>	1	Random hot deck	Random number	Random number
	2	Nearest neighbor	Prior Month Sales	Random number
	3	Propensity	Prior Month Sales	Prior months sales (descending)
	4	Propensity	Prior Month Sales and Number of Identified Industries for Reporting Unit	Random number
	5	Propensity	Prior Month Sales and Number of Identified Industries for Reporting Unit	Prior month sales (descending)
<b>Optimal</b>	1	Propensity	Prior Month Sales	N/A
	2	Propensity	Prior Month Sales and Number of Identified Industries for Reporting Unit	N/A

# Evaluation Statistics: Mean Absolute Error

- **Mean Absolute Error (MAE)**

$$MAE_t^{am} = \sum_{i=1}^{n'_{rt}} \left| x_{t,r(i)} - \left( \frac{X_{t,d(i)}^{am}}{X_{t-1,d(i)}^{am}} \right) x_{t-1,r(i)} \right| / n'_{rt}$$

The diagram illustrates the components of the MAE formula. A blue oval labeled "Truth" has an arrow pointing to the  $x_{t,r(i)}$  term in the formula. Another blue oval labeled "Imputed value" has a bracket pointing to the entire term in parentheses:  $\left( \frac{X_{t,d(i)}^{am}}{X_{t-1,d(i)}^{am}} \right) x_{t-1,r(i)}$ .

measures the average magnitude of the error per imputed unit.

# Evaluation Statistics: Relative Bias

- ***Unconditional Relative Bias (URB)*** – measures the overall effect of the imputation error on the tabulated estimates.

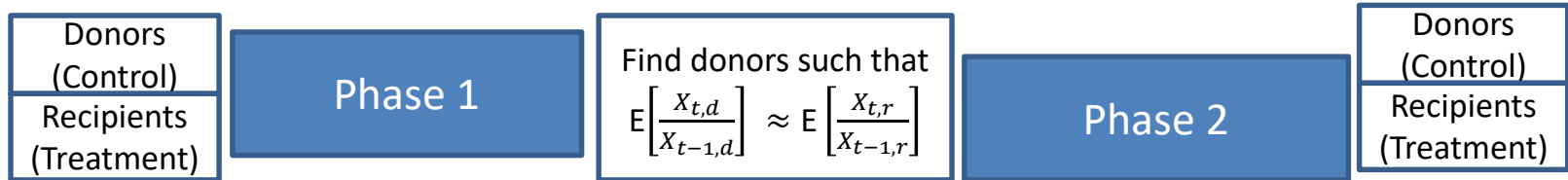
$$RB_t^{am} = \frac{\hat{X}_t^{am}}{X_t} - 1$$

- ***Conditional Relative Bias (CRB)*** – provides the direction of the imputation bias for the imputed units and gives some indication of the magnitude. Extremely sensitive to size.

$$CRB_t^{am} = \frac{\hat{X}_t^{am(R)}}{X_t^R} - 1$$



# Two Phases to our Research



- Find which matching applications are most effective in selecting donors (imputation constant)
  - Donated ratio - current month/prior month
- Compare statistical performance of the recommended matching algorithm from Phase 1 (imputation varied, matching constant)
  - Donated ratios from 1 year ago (seasonality)
  - Donated ratios from most recent calendar with the same working day composition (seasonality & trading day)

# One Match Variable Versus Two

- Chi-square tests for independence
- Treatment = two match variables
- Control = one match variable
- Optimal and Greedy match – no improvement with two

# Phase 1 Summary

Looking at MAE and CRB

- Random Hot Deck worst performance
- Nearest Neighbor slight underperformance compared to Optimal and Greedy
- Greedy and Optimal similar performance
  - Greedy - needed to “trick” the code
- Phase 2 will focus on Optimal Matching

# Phase 2: Selection of Hot Deck Donor Pool

Ratio	Min.	Q1	Med.	Q3	Ma x
Donors (1 Year Ago) to Recipients	0.89	1.69	2.14	3.19	5.58
Donors (5 Years Ago) to Recipients	0.55	0.97	1.38	1.69	2.70

# Phase 2: Chi-Square Test for Independence to Assess Treatment Effect (Donor Choice)

	1 year ago outperformed	5 years ago outperformed	Tie between the 2 treatments
MAE	17	11	2
URB	16	9	5

- Example where p-value is misleading
  - There is a an effect overall...but it ignores differences within industries

# Concluding Remarks

- Optimal matching effective
  - Parsimonious model works
  - No need for a single score in our application
- Challenge in determining how to use donors
  - No one-size-fits-all model with for choosing ratios
  - Considering alternative calendar adjustments

# Related Research

- Comparison to other missing data treatments as part of a larger study
  - 10:30 tomorrow morning in 145AB Nikki Czaplicki is presenting “Finding an Estimator that Minimizes Revisions in a Monthly Indicator Survey”

# Thank you

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